

Operators (2A)

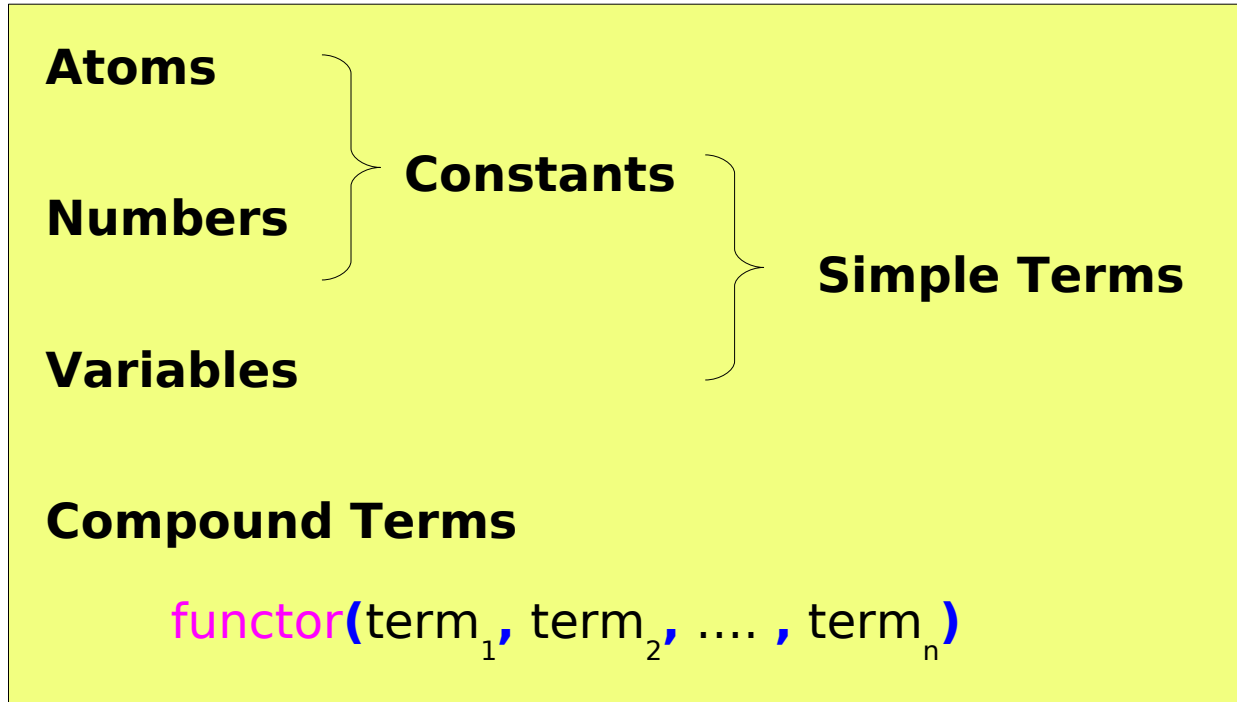
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Terms (1)



**A term without
any variables**

A ground term

Terms (2)

Atoms

A string of characters
Characters enclosed in single quotation
A string of special characters

Numbers

Integer numbers

Variables

Variables:
Starting with a capital letter or _
Anonymous variable _ :
Multiple occurrence in one expression are
assumed to be distinct

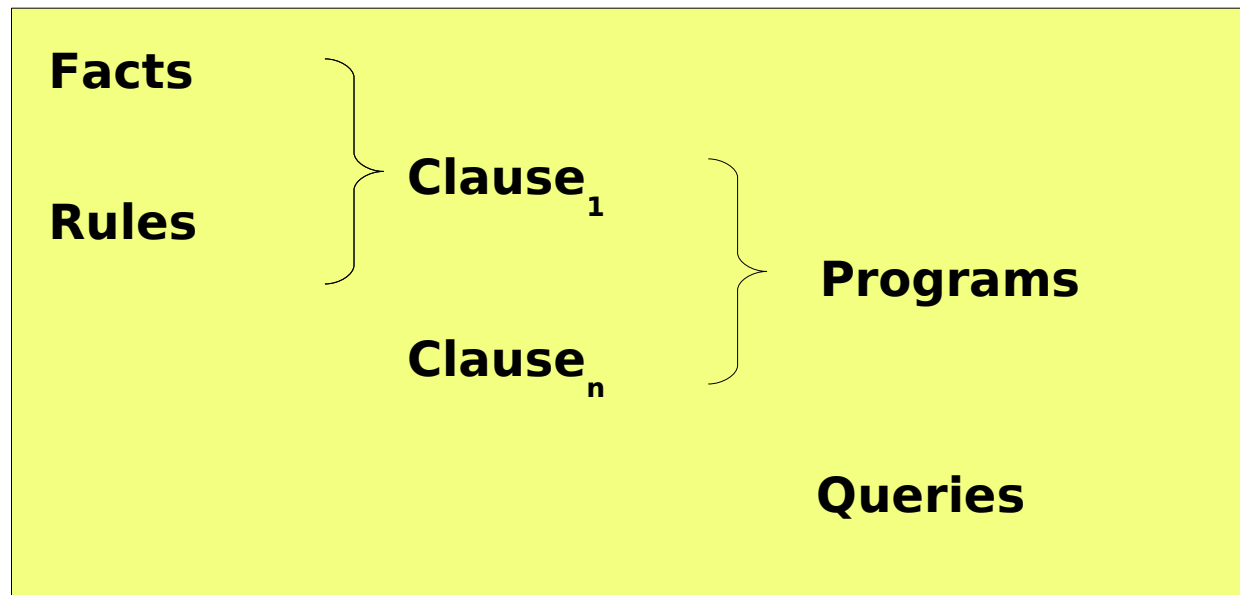
Compound Terms

should be no space

an atom

functor(term₁, term₂, , term_n)

Clause



Facts A predicate followed by a dot.
 A functor, an atom

Rules { **a head :-** A predicate (a functor, an atom)
 { **a body .** A sequence of predicates separated by , 's

Precedence

Every operator

associated with an integer number

SWI-prolog

[0, 1200]

higher
priority lower
priority

* → 400

+ → 500

a term → If its principle functor is an operator
then the precedence of an operator
Else the precedence is defined as 0

5 + 7 precedence of 500

5*5 + 7*7 precedence of 500

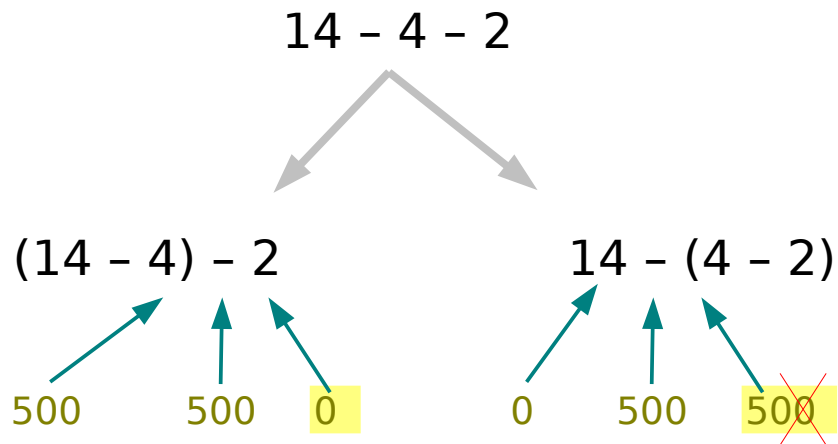
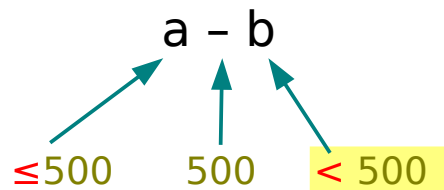
sqrt(5 + 7) precedence of 0

man precedence of 0

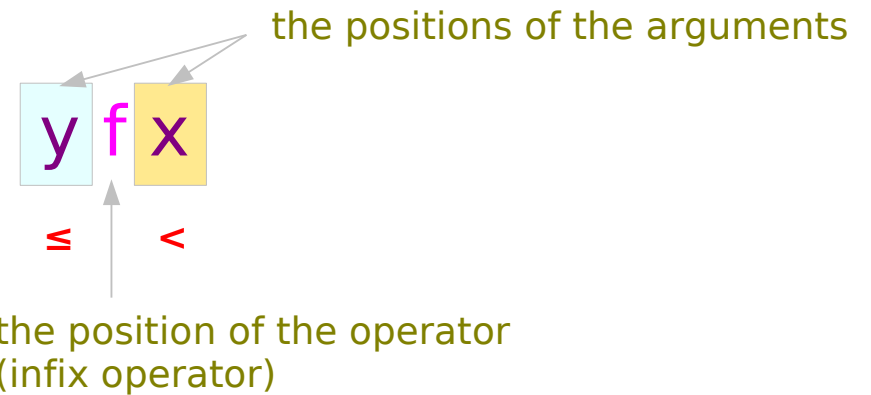
3 * +(5, 7) precedence of 400

Associativity

- Infix operators
- Prefix operators
- Postfix operators



Left Associative operator



the precedence of $x <$ the precedence of f
 the precedence of $y \leq$ the precedence of f

$$2 * 3 * 4 * 5$$

$$((2 * 3) * 4) * 5$$

Left Associative operator

Disjunction Operator

{ Infix operators
Prefix operators
Postfix operators

a, b, c, d

a, (b, c, d)

a, (b, (c, d))

Right Associative operator

$2 ** 3 ** 4 ** 5$

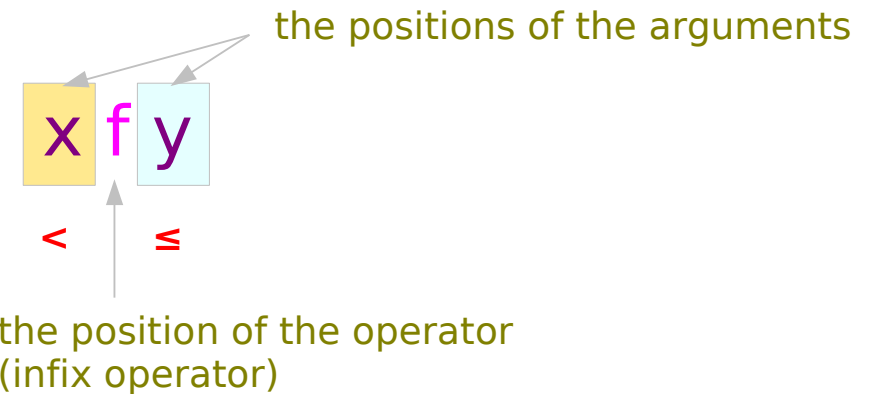
$2 ^ 3 ^ 4 ^ 5$

$2 ^ (3 ^ 4 ^ 5)$

$2 ^ (3 ^ (4 ^ 5))$

SWI-prolog $\wedge \rightarrow **$

Right Associative operator



the disjunction operator ; or |

```
head :- body1.
```

```
head :- body2.
```

```
↔ head :- body1 ; body2.
```

```
head :- b1 ; b2; b3; b4.
```

```
head :- (b1 ; (b2; b3; b4)).
```

```
head :- (b1 ; (b2; (b3; b4))).
```

Right Associative operator

Comma Operator

Comma Sequences

No empty sequence

The shortest sequence

- one element

```
:- op(1000, xfy, ',');
```

```
?- (H, T) = (1,2,3);
```

```
H = 1
```

```
T = 2, 3, 4
```

```
?- (a) = a.
```

```
Yes
```

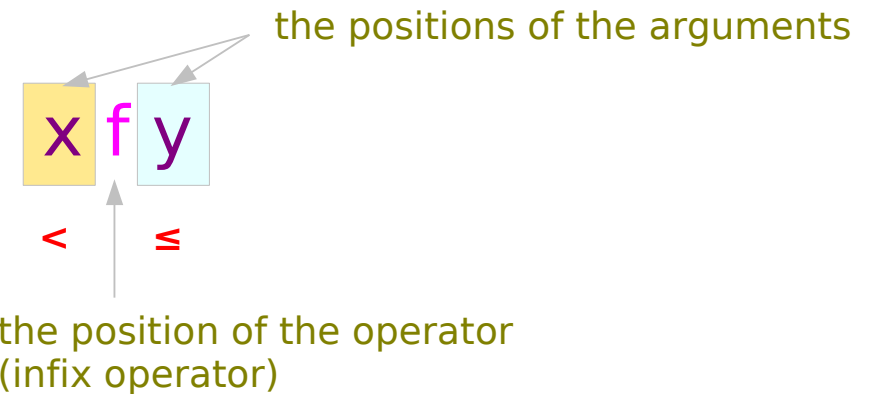
```
?- (A,B,C) = (1,2,3,4,5,6).
```

```
A = 1
```

```
B = 2
```

```
C = 3,4,5
```

Right Associative operator



Prolog clauses use comma sequences.

```
(A,B,C) = (1,(2,(3,4,5,6)))
```

Negation As Failure

```
bachelor(P) :- male(P), not(married(P)).  
male(henry).  
male(tom).  
married(tom).
```

```
not not not married(P)  
not (not not married(P))  
not (not (not married(P)))  
not (not (not (married(P)))
```

Right Associative operator

```
?- bachelor(henry).  
Yes
```

```
?-bachelor(tom).  
No
```

```
?-bachelor(Who).  
Who=henry;  
No
```

```
?- not(married(Who)).  
No.
```

For the variable binding **Who**=tom,
married(**Who**) succeeds
not(married(**Who**)) fails

Negative goals with variables **cannot**
be expected to produce **bindings** of
the variables **for which the goals fails**

NAF (Negation As Failure)

PLANNER

if (**not** (goal p)), then (assert $\neg p$)

If **the goal to prove p** fails, then assert $\neg p$

If NAF used to derive **not p** (**p is assumed not to hold**) from failure to derive p

Not p can be different from the statement $\neg p$ of the logical negation of p , depending on the **completeness** of the inference algorithm and thus also on the formal logic system

Prolog

NAF literals of the form of **not p** can occur in the body of clauses

Can be used to derive other NAF literals

$$\begin{aligned} p &\leftarrow q \wedge \text{not } r \\ q &\leftarrow s \\ q &\leftarrow t \\ t & \end{aligned}$$

Infix Operators

INFIX Operators

$y f x$

left-associative

$+, -, *, /$

$x f y$

right-associative

$,$ (subgoals)

$x f x$

non-associative

$=, is, <$ (no nesting)

~~$y f y$~~

Not possible

Prefix & Postfix Operators

PREFIX Operators

$f\ x$ non-associative - (--3 not possible)

$f\ y$ right-associative , (subgoals)

POSTFIX Operators

$x\ f$ non-associative

$y\ f$ left-associative

Operator Examples

?- current_op(Precedence, Associativity, *).
Precedence = 400
Associativity = yfx left-associative
Yes

?- current_op(Precedence, Associativity, **).
Precedence = 200
Associativity = xfx ; non-associative
No

?- current_op(Precedence, Associativity, -).
Precedence = 500
Associativity = yfx ; left-associative
Precedence = 500
Associativity = fx ;
No

?- current_op(Precedence, Associativity, <).
Precedence = 700
Associativity = xfx ; non-associative
No

?- current_op(Precedence, Associativity, =).
Precedence = 700
Associativity = xfx ; non-associative
No

?- current_op(Precedence, Associativity, :-).
Precedence = 1200
Associativity = xfx ; non-associative
Precedence = 1200
Associativity = fx ;
No

Operator Examples

<code>:=</code>	<code>xfx, fx</code>	non-associative		Large P
<code>?-</code>	<code>fx</code>	non-associative		
<code>;</code>	<code>xfy</code>	right associative		
<code>,</code>	<code>xfy</code>	right associative		
<code>not</code>	<code>fy</code>	right associative		
<code>is, =..., <, etc.</code>	<code>xfx</code>	non-associative		
<code>+, -</code>	<code>yfx, fx</code>	left associative		
<code>*, /</code>	<code>yfx</code>	left associative		
<code>^</code>	<code>xfy</code>	right associative		Small P

References

- [1] U. Endriss, "Lecture Notes : Introduction to Prolog Programming"
- [2] <http://www.learnprolognow.org/> Learn Prolog Now!
- [3] http://www.csupomona.edu/~jrfisher/www/prolog_tutorial
- [4] www.cse.unsw.edu.au/~billw/cs9414/notes/prolog/intro.html