

# Rectifier (H.1)

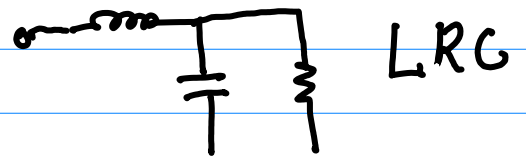
20170405

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# Filter

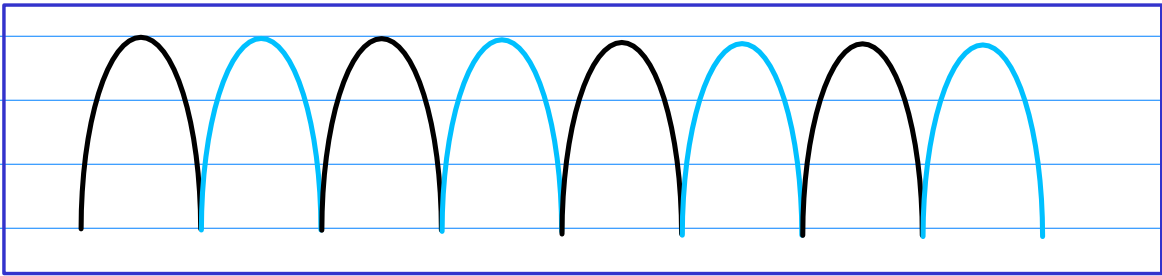
① Choke-input Filter



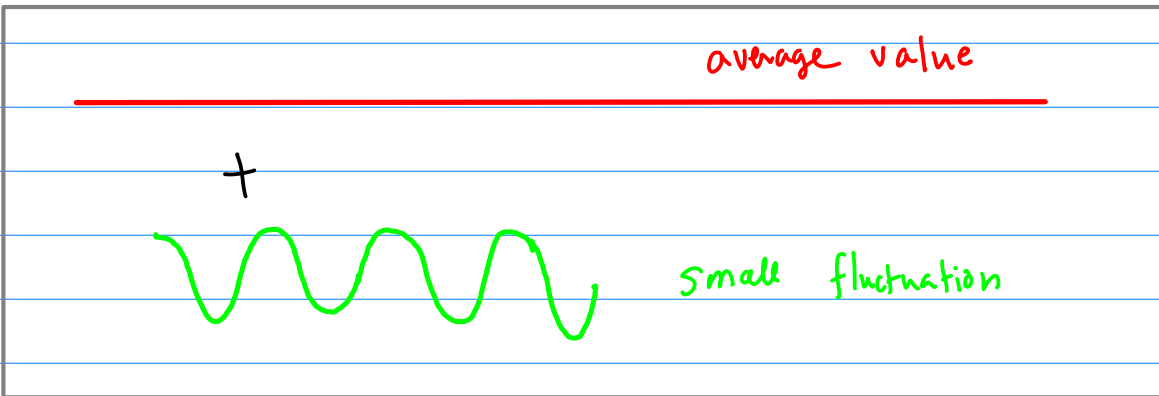
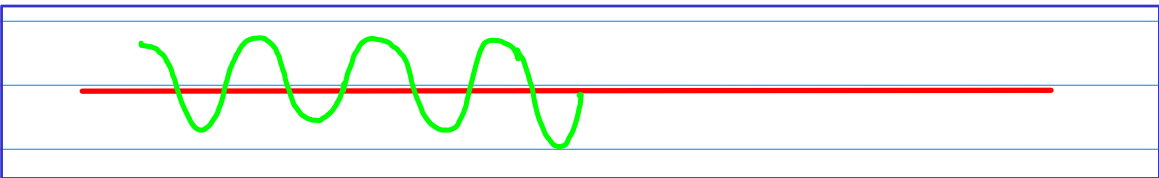
② Capacitor-input Filter



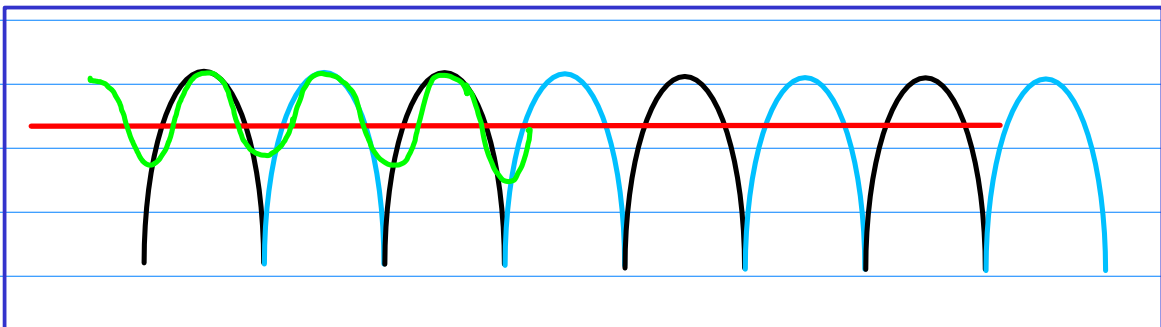
full-wave rectifier output

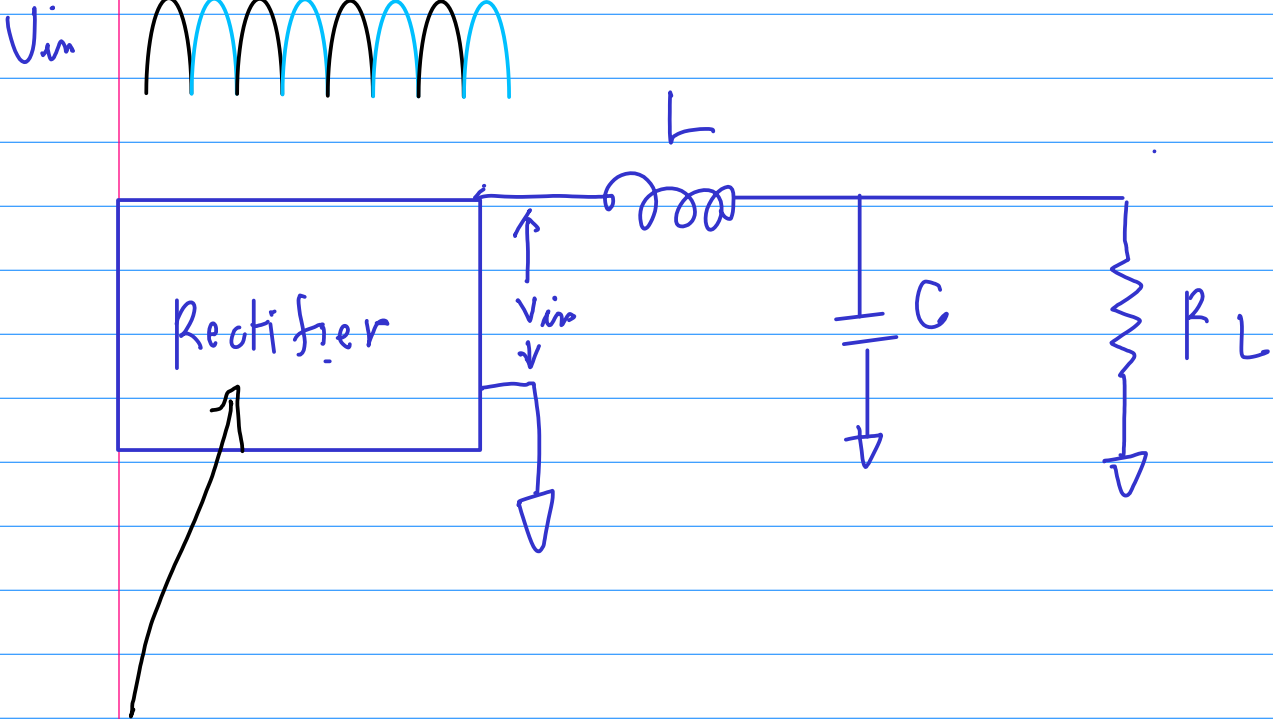


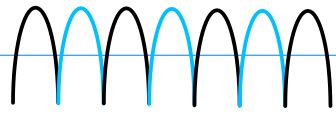
View this as follows      DC + AC



Superposition

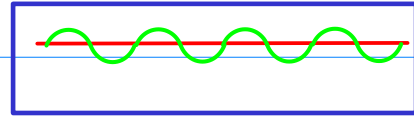
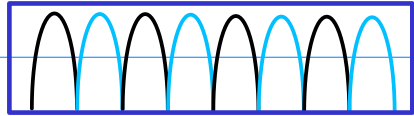




- ① Full-wave Rectifier
  - ② Bridge Rectifier
- } 

$$U_{in} = U_{in(dc)} + U_{(ac)}$$

$U_{in}$

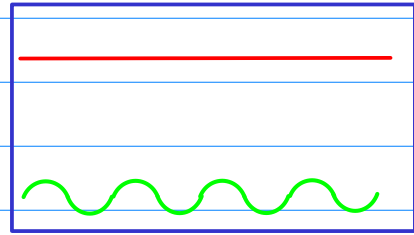


=

$U_{in(dc)}$

+

$U_{(ac)}$



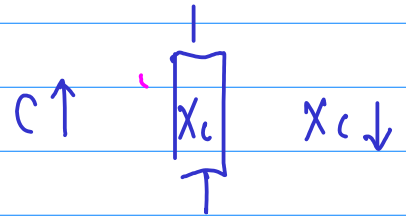
$\Rightarrow$

$T$

$$\omega = 2\pi f = \frac{2\pi}{T}$$

$$X_C = \frac{1}{2\pi f C}$$

$$X_L = 2\pi f L$$



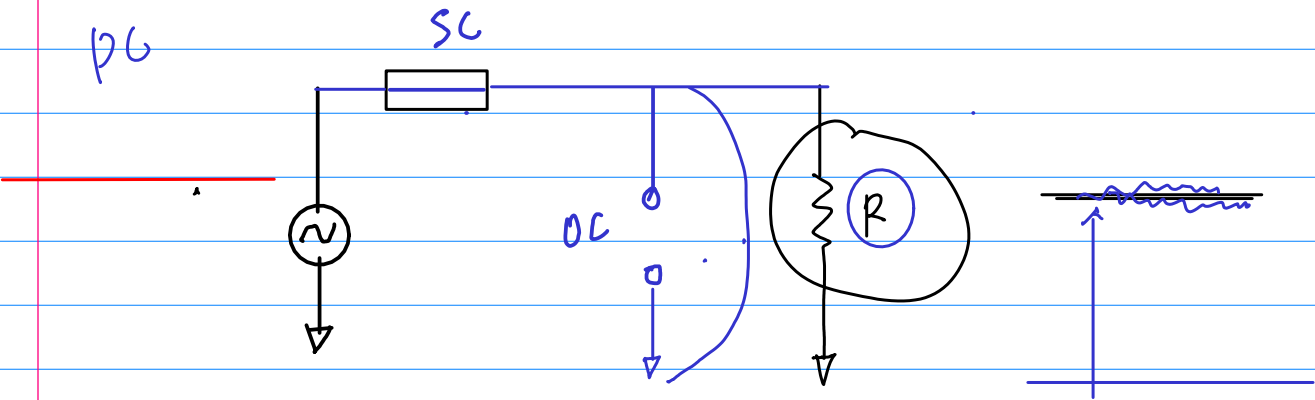
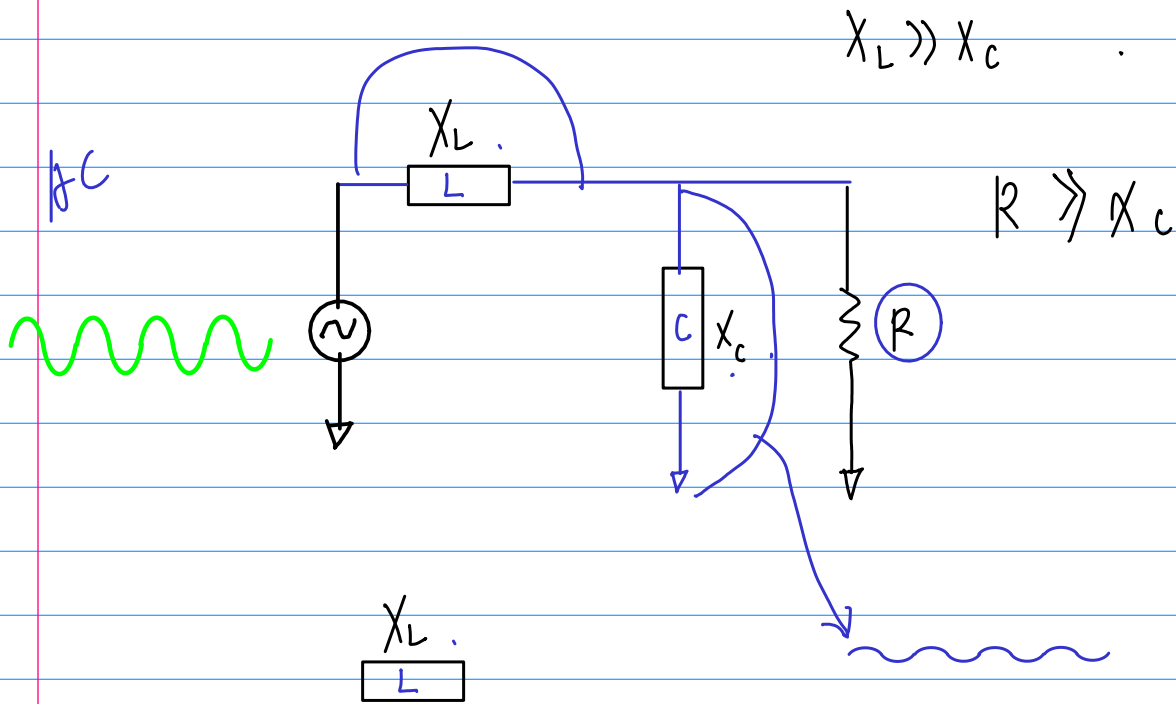
$$X_L \gg X_C$$

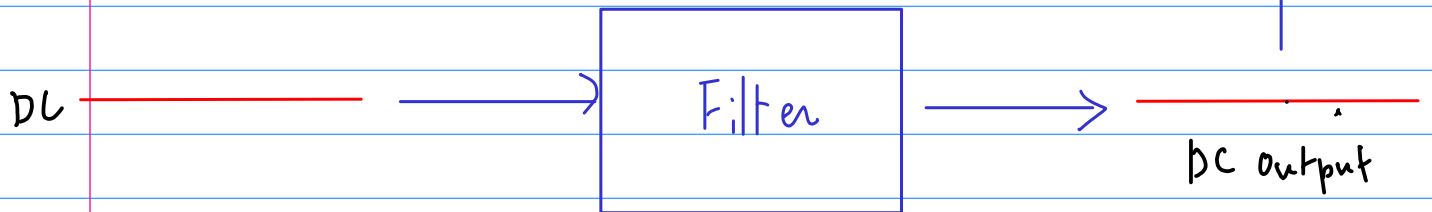
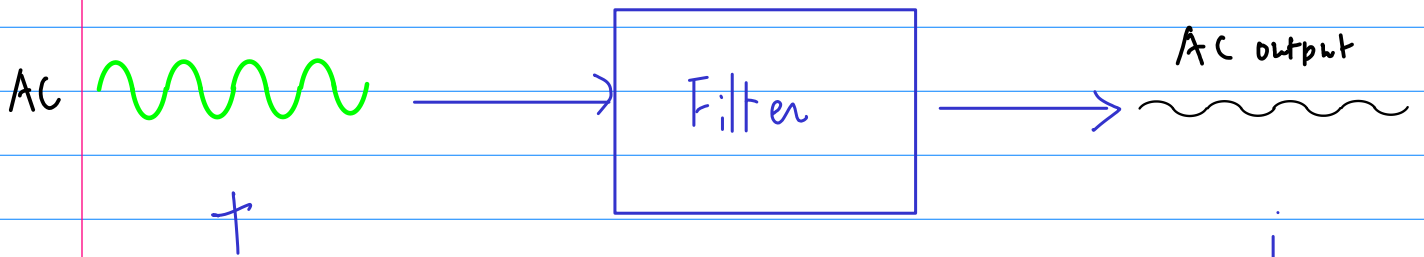
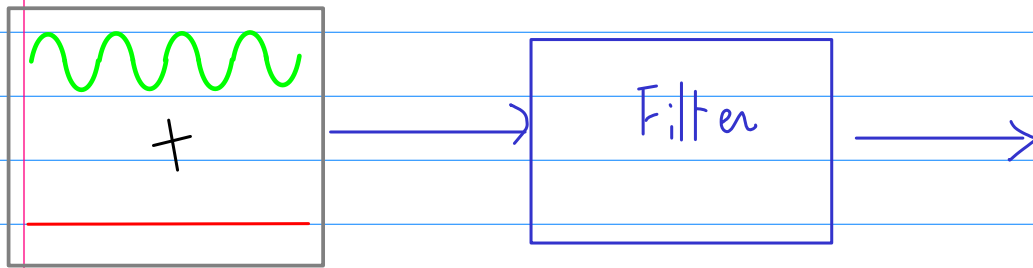
$$R \gg X_C$$

$L \uparrow$

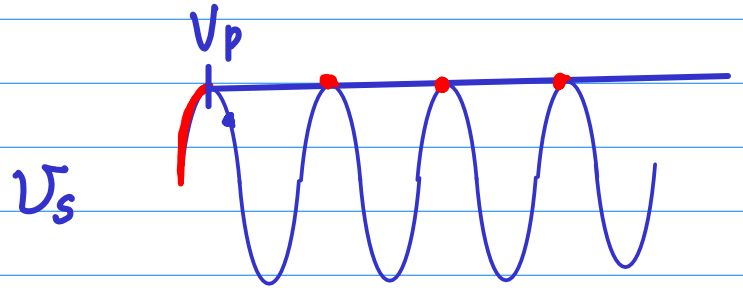
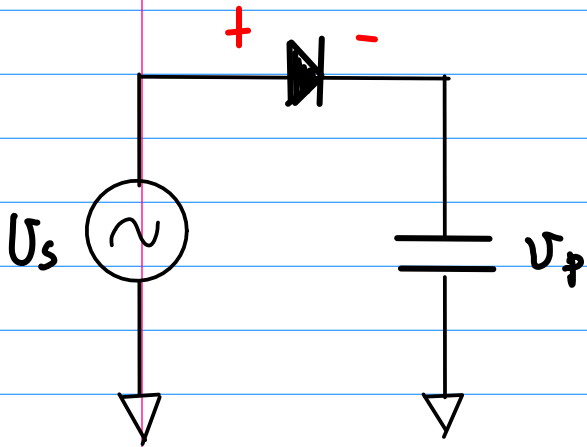
$X_L$

$X_L \uparrow$



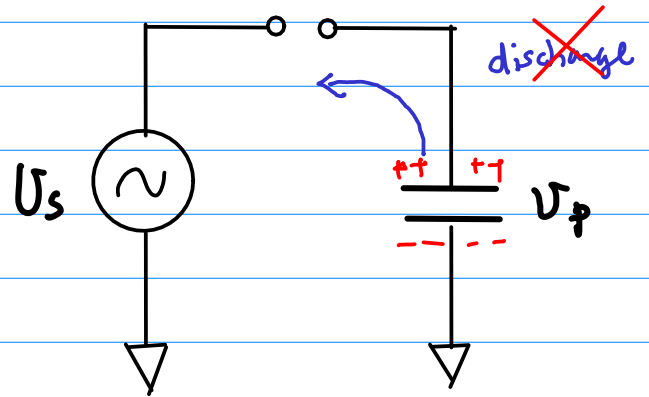
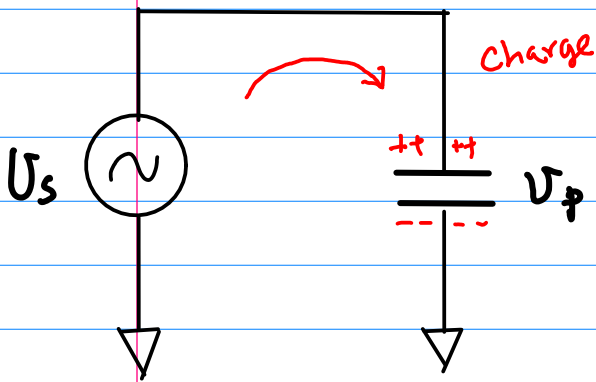


# Capacitor - Input Filter

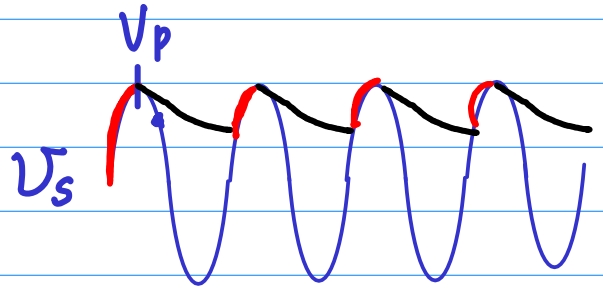
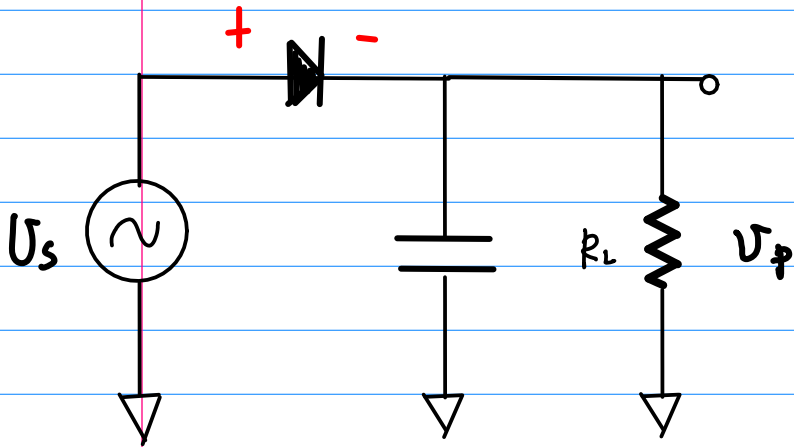


$$U_s \geq U_p$$

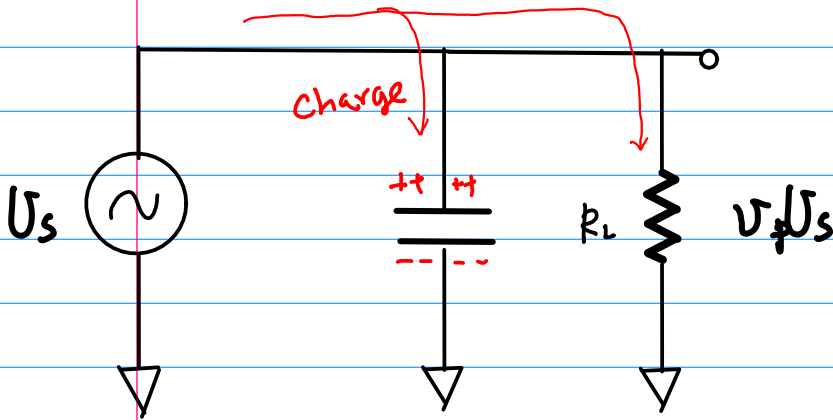
$$U_s < U_p$$



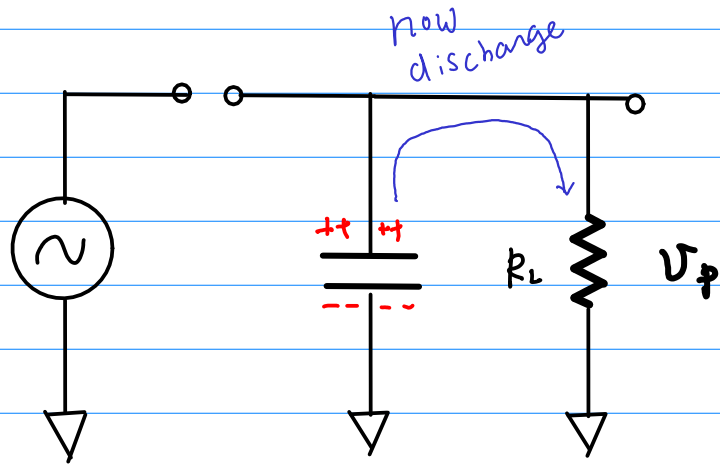


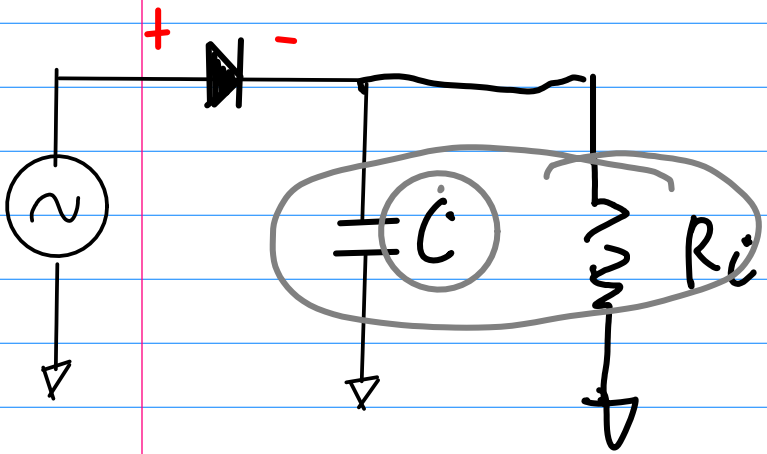


$U_s \geq U_p$

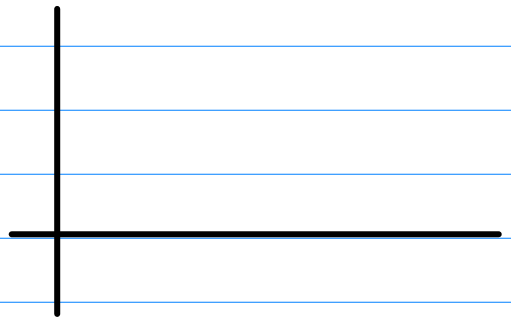
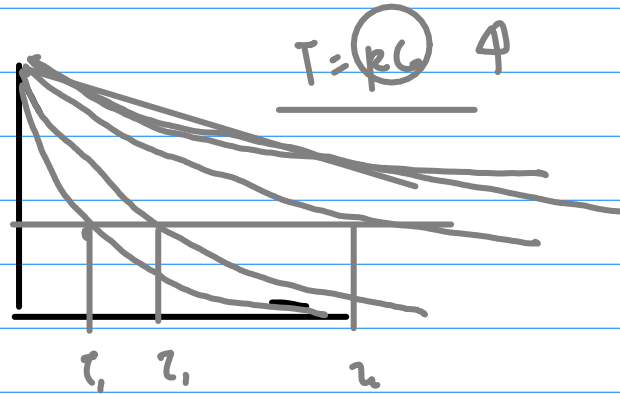


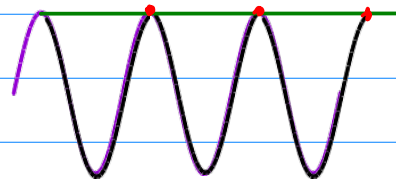
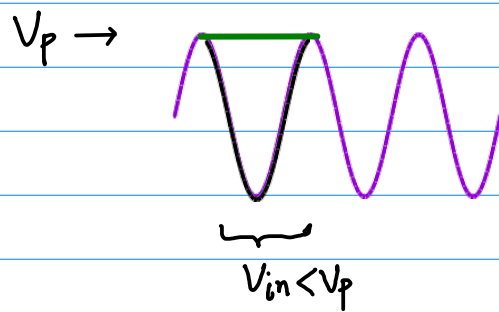
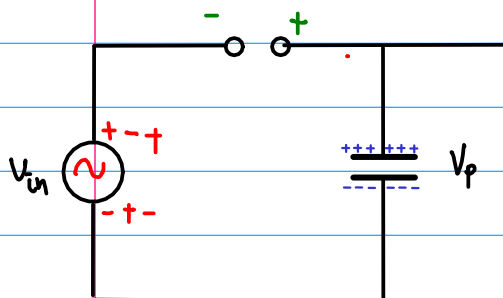
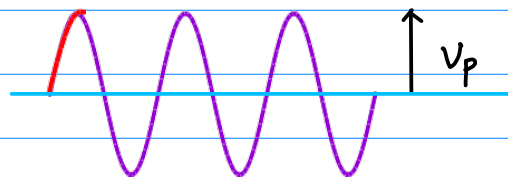
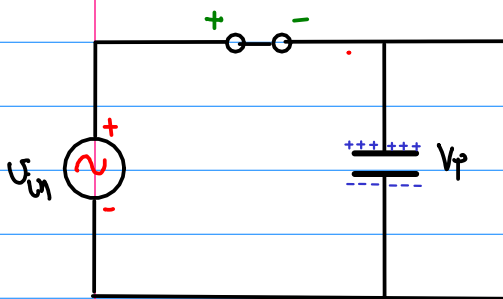
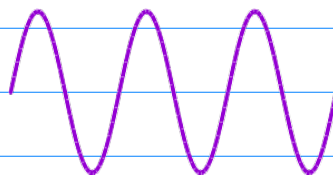
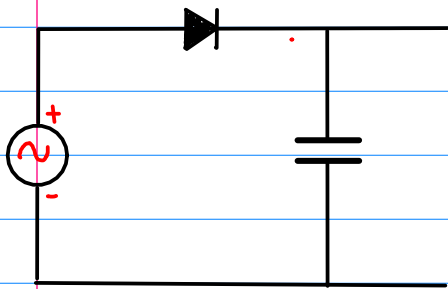
$U_s < U_p$





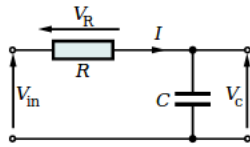
$e^{-t}$





# Transient Response

## Charge

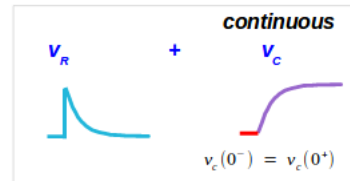
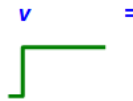


$$i_c = C \cdot \frac{dv_c}{dt}$$

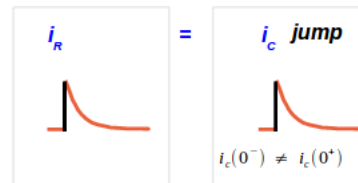
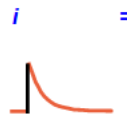
unyielding voltage

current jump

the capacitor voltage slowly follows the shape of the applied step input voltage



the capacitor current changes abruptly by the applied step input voltage and then slowly becomes zero

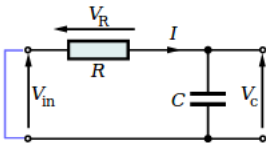


Capacitor

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## Discharge

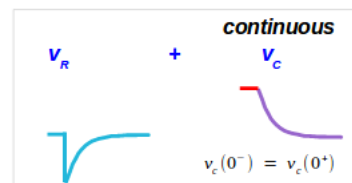


$$i_c = C \cdot \frac{dv_c}{dt}$$

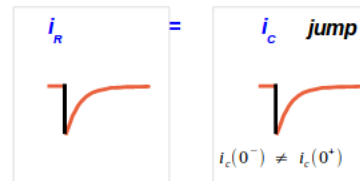
unyielding voltage

current jump

the capacitor voltage slowly follows the shape of the applied step input voltage



the capacitor current changes abruptly by the applied step input voltage and then slowly becomes zero

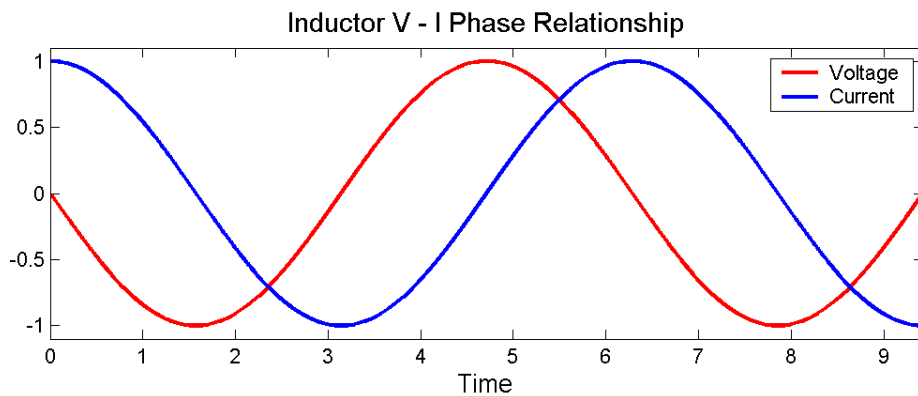
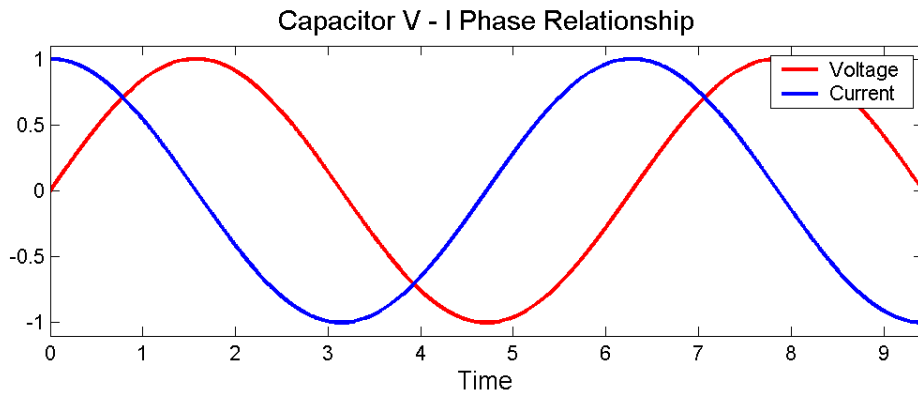


Capacitor

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# Steady State



[https://en.wikipedia.org/wiki/Electrical\\_impedance](https://en.wikipedia.org/wiki/Electrical_impedance)

The phase angles in the equations for the impedance of capacitors and inductors indicate that the voltage across a capacitor *lags* the current through it by a phase of  $\pi/2$ , while the voltage across an inductor *leads* the current through it by  $\pi/2$ . The identical voltage and current amplitudes indicate that the magnitude of the impedance is equal to one.

### Capacitor [\[ edit \]](#)

For a capacitor, there is the relation:

$$i_C(t) = C \frac{d v_C(t)}{d t}$$

Considering the voltage signal to be

$$v_C(t) = V_p \sin(\omega t)$$

it follows that

$$\frac{d v_C(t)}{d t} = \omega V_p \cos(\omega t)$$

and thus

$$\frac{v_C(t)}{i_C(t)} = \frac{V_p \sin(\omega t)}{\omega V_p C \cos(\omega t)} = \frac{\sin(\omega t)}{\omega C \sin\left(\omega t + \frac{\pi}{2}\right)}$$

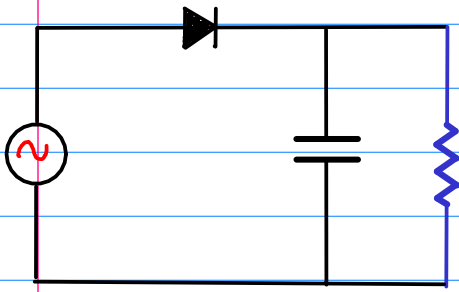
This says that the ratio of AC voltage amplitude to AC current amplitude across a capacitor is  $\frac{1}{\omega C}$ , and that the AC voltage lags the AC current across a capacitor by 90 degrees (or the AC current leads the AC voltage across a capacitor by 90 degrees).

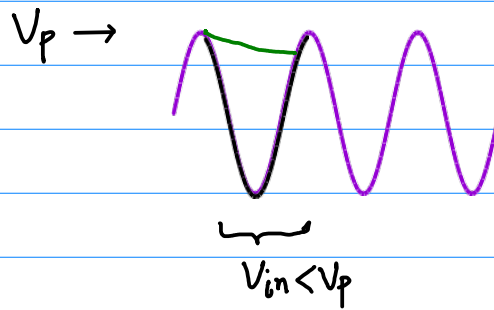
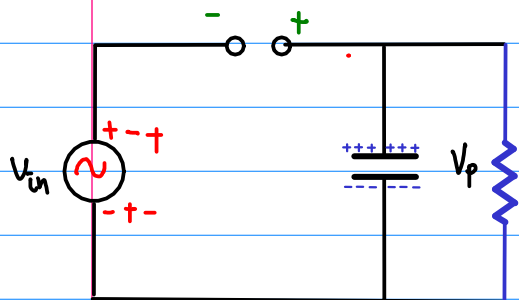
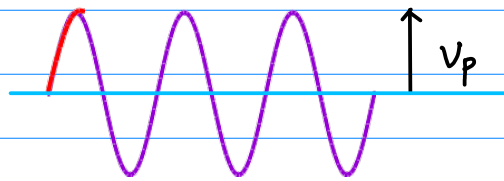
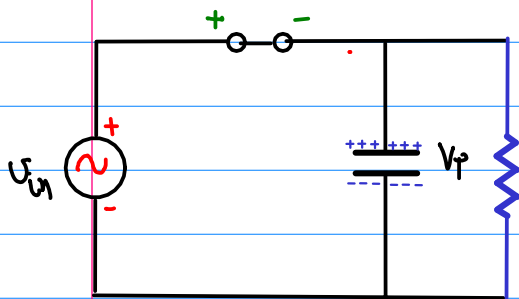
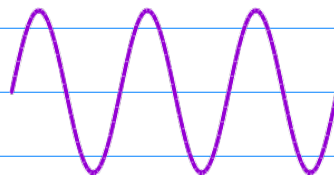
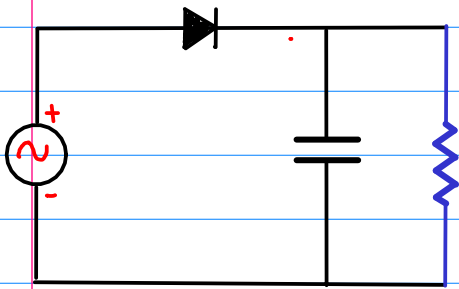
This result is commonly expressed in **polar form** as

$$Z_{\text{capacitor}} = \frac{1}{\omega C} e^{-j\frac{\pi}{2}}$$

or, by applying Euler's formula, as

$$Z_{\text{capacitor}} = -j \frac{1}{\omega C} = \frac{1}{j\omega C}$$





Charge discharge

