

	x	y	z	Minterm		Maxterm	
				term		term	
0	0	0	0	$x'y'z'$	m0	$(x+y+z)$	M0
1	0	0	1	$x'y'z$	m1	$(x+y+z')$	M1
2	0	1	0	$x'yz'$	m2	$(x+y'+z)$	M2
3	0	1	1	$x'yz$	m3	$(x+y'+z')$	M3
4	1	0	0	$xy'z'$	m4	$(x'+y+z)$	M4
5	1	0	1	$xy'z$	m5	$(x'+y+z')$	M5
6	1	1	0	$xyz'$	m6	$(x'+y'+z)$	M6
7	1	1	1	$xyz$	m7	$(x'+y'+z')$	M7

$$\begin{array}{l} x=0 \text{ and } y=0 \text{ and } z=0 \\ x=0 \text{ and } y=0 \text{ and } z=1 \end{array} \left| \begin{array}{l} \longleftrightarrow \\ \longleftrightarrow \end{array} \right. \begin{array}{l} x'y'z'=1 \\ x'y'z=1 \end{array}$$

$$\begin{array}{l} x=0 \text{ and } y=0 \text{ and } z=0 \\ x=0 \text{ and } y=0 \text{ and } z=1 \end{array} \left| \begin{array}{l} \longleftrightarrow \\ \longleftrightarrow \end{array} \right. \begin{array}{l} (x+y+z)=0 \\ (x+y+z')=0 \end{array}$$

A	B	C	D	minterm	maxterm
0	1	1	0	$A'BCD'$	$A+B'+C'+D$
1	0	1	1	$AB'CD$	$A'+B+C'+D'$

$$f1 = x'y'z + xy'z' + xyz = m1 + m4 + m7$$

In order  $f1$  has the value of 1, the following minterms should be included ( $m1=1$ ) or ( $m4=1$ ) or ( $m7=1$ )

$m0, m2, m3, m5, m6$

$$m0 + m2 + m3 + m5 + m6 = x'y'z' + x'yz' + x'yz + xy'z + xyz' = f1'$$

$$(m0 + m2 + m3 + m5 + m6)' = (x'y'z' + x'yz' + x'yz + xy'z + xyz')' = (f1)'$$

## De Morgan's law

$$f1 = (m0 + m2 + m3 + m5 + m6)' = (x'y'z' + x'yz' + x'yz + xy'z + xyz)'$$

$$f1 = (m0' m2' m3' m5' m6') = (x'y'z')' (x'yz')' (x'yz)' (xy'z)' (xyz)'$$

## De Morgan's law

$$f1 = (m0' m2' m3' m5' m6') = (x+y+z) (x+y'+z) (x+y'+z') (x'+y+z') (x'+y'+z)$$

$$f1 = (m0' m2' m3' m5' m6') = (M0) (M2) (M3) (M5) (M6)$$

$$f1 = (m0' m2' m3' m5' m6') = (m0=0) \wedge (m2=0) \wedge (m3=0) \wedge (m5=0) \wedge (m6=0)$$

in order to **f1** has the value of **1**,  
the following **minterms** should not be included  
m0, m2, m3, m5, m6

$$f1 = (M0) (M2) (M3) (M5) (M6) = (M0=1) \wedge (M2=1) \wedge (M3=1) \wedge (M5=1) \wedge (M6=1)$$

in order to **f1** has the value of **1**,  
the following **maxterms** should not be included  
M0, M2, M3, M5, M6

**Sum** of Product      Sum of Minterms

$$f1 = x'y'z + xy'z' + xyz = m1 + m4 + m7$$

SoP

$$f1 = (m0' m2' m3' m5' m6') = M0 M2 M3 M5 M6 \\ = (x+y+z) (x+y'+z) (x+y'+z') (x'+y+z') (x'+y'+z)$$

Product of **Sum**      Product of Maxterms

Ex 2.4

$$F = A + B'C$$

$f = A + B + C$

$$A = A(B + B') = AB + AB' = AB(C+C') + AB'(C+C') \\ = ABC + ABC' + AB'C + AB'C' = m_7 + m_6 + m_5 + m_4$$

$$B'C = (A+A')B'C = AB'C + A'B'C = m_5 + m_1 \\ = m_1 + m_4 + m_5 + m_6 + m_7$$

$$F(A, B, C) = \Sigma(1, 4, 5, 6, 7)$$

	x	y	z	term
0	0	0	0	0
1	0	0	1	1
2	0	1	0	0
3	0	1	1	0
4	1	0	0	1
5	1	0	1	0
6	1	1	0	0
7	1	1	1	1

$$m_1 + m_4 + m_7 = f_1$$

$$m_0 + m_2 + m_3 + m_5 + m_6 = f_1'$$





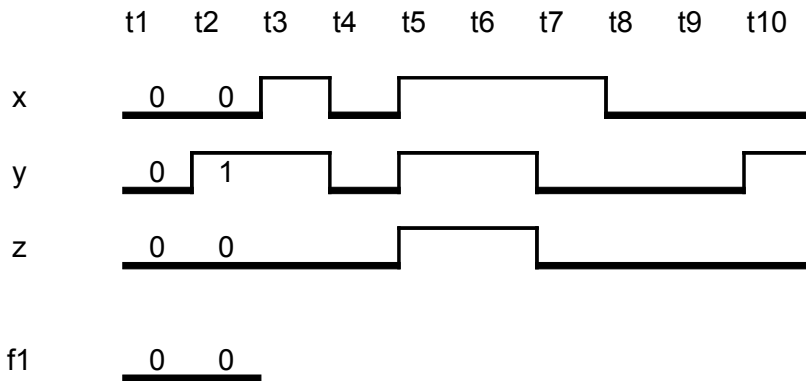


0	0	0	1	0	1	1	multiplicand multiplier	
		x	0	1	0	1		
0	0	0	1	0	1	1		
0	0	0	0	0	0	0		
0	1	0	1	1	0	0		
0	0	0	0	0	0	0		
0							1	
	1	1	0	1	1	1		
	32	16		7				

0xFF	1	1	1	1	1	1	1	1
0x01	0	0	0	0	0	0	0	1
0x23	0	0	1	0	0	0	1	1
& 0x01	0	0	0	0	0	0	0	1
	0	0	0	0	0	0	0	1

HW

(1) Complete the waveform of the function f1



$$f1 = x'y'z + xy'z' + xyz = m1 + m4 + m7$$

