

Algorithms - Bubble Sort (1B)

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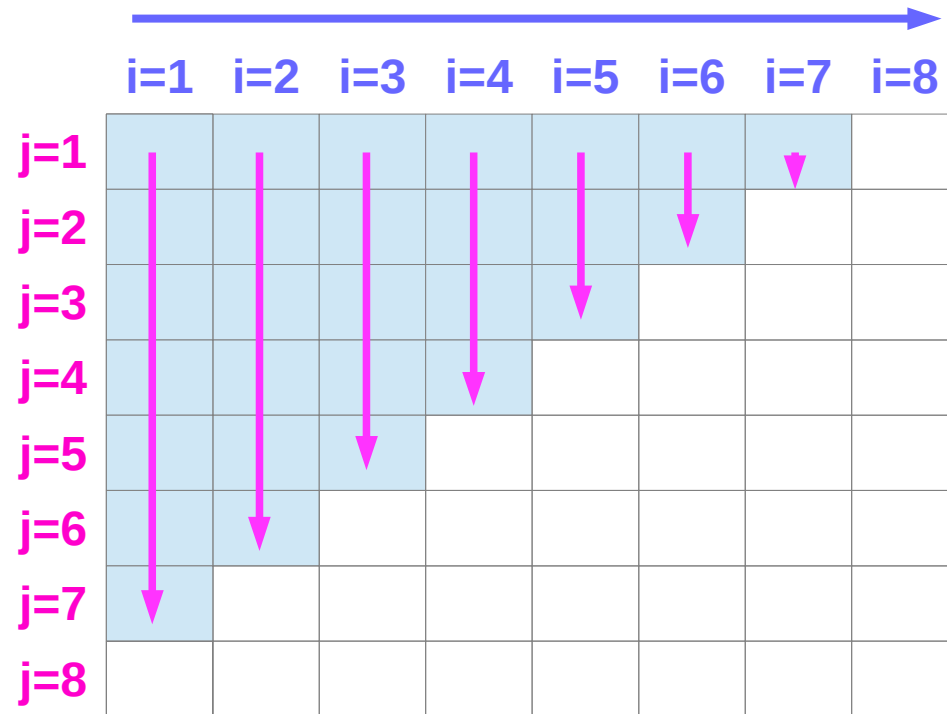
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Bubble Sort Algorithm

```
procedure bubblesort( $a_1, \dots, a_n$  : real numbers with  $n \geq 2$ )  
for  $i := 1$  to  $n-1$   
    for  $j := 1$  to  $n - i$   
        if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$   
{ $a_1, \dots, a_n$  is in increasing order}
```

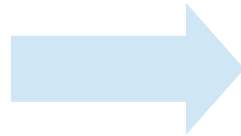
Nested loop iterations



```
for  $i := 1$  to  $n-1$   
  for  $j := 1$  to  $n - i$ 
```

Input and Output

a_1	44
a_2	55
a_3	22
a_4	88
a_5	66
a_6	11
a_7	77
a_8	33

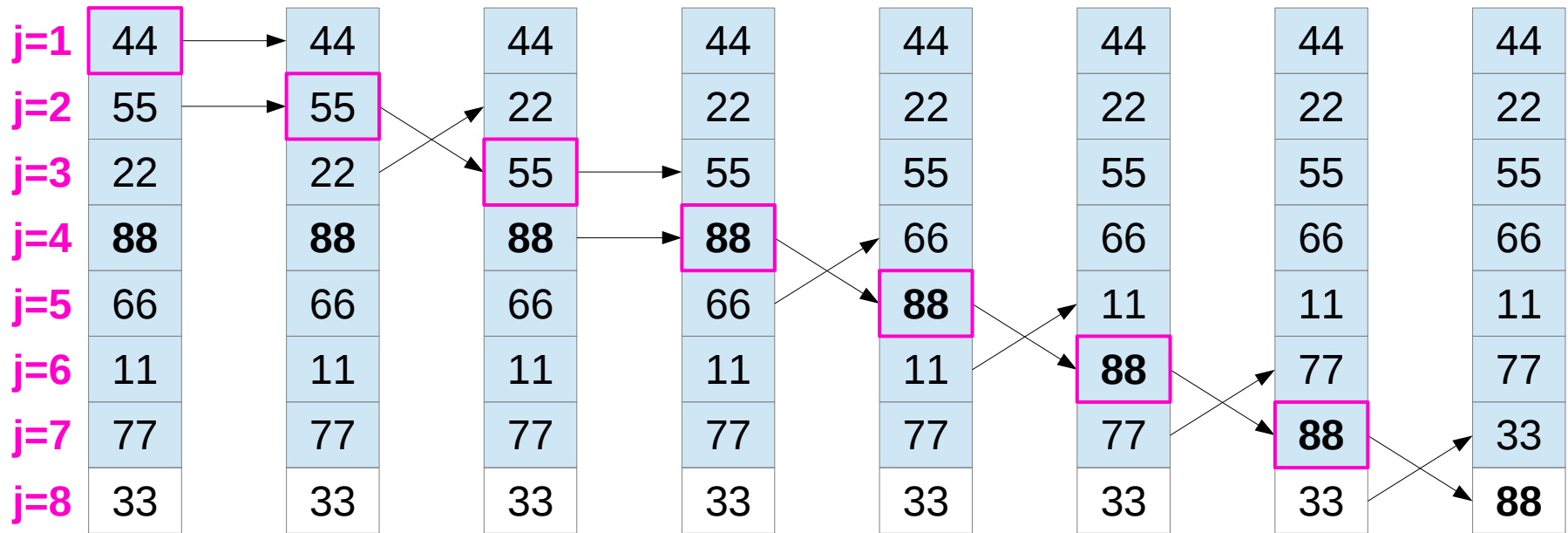


a_1	11
a_2	22
a_3	33
a_4	44
a_5	55
a_6	66
a_7	77
a_8	88

a_1, \dots, a_n : real numbers
with $n \geq 2$

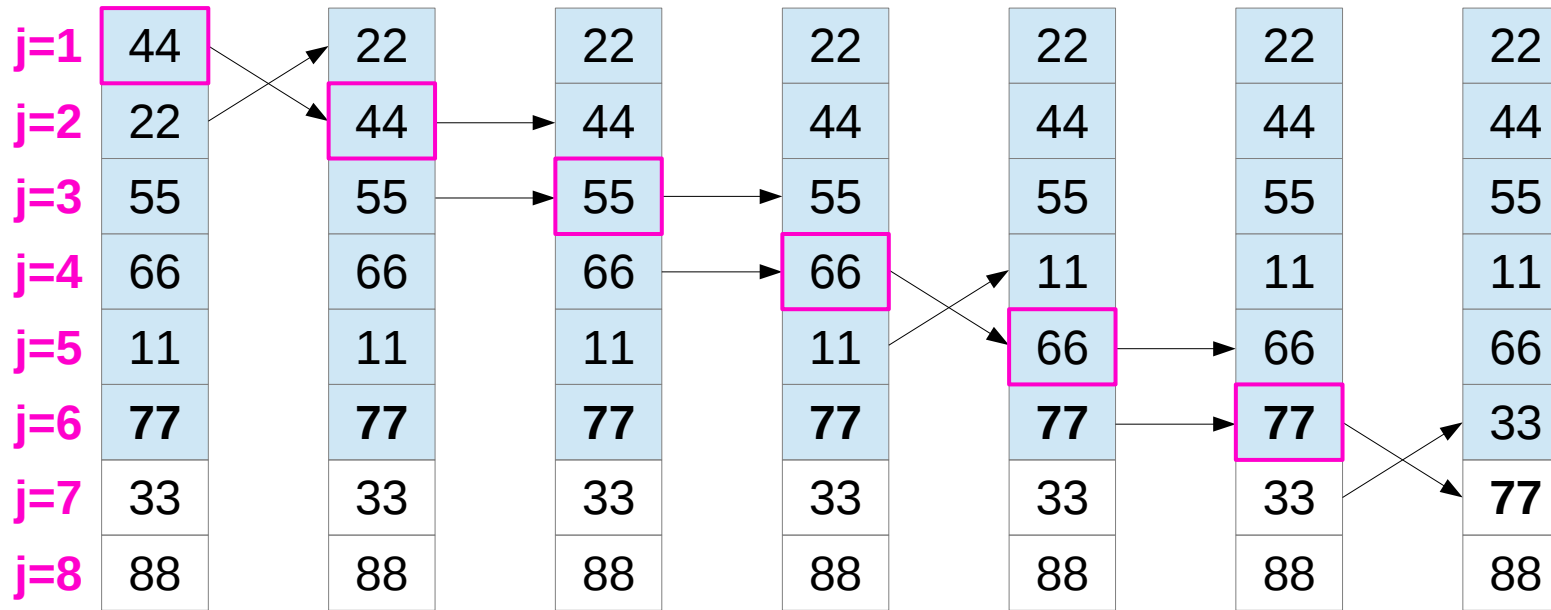
$\{a_1, \dots, a_n$ is in increasing order}

Step i=1



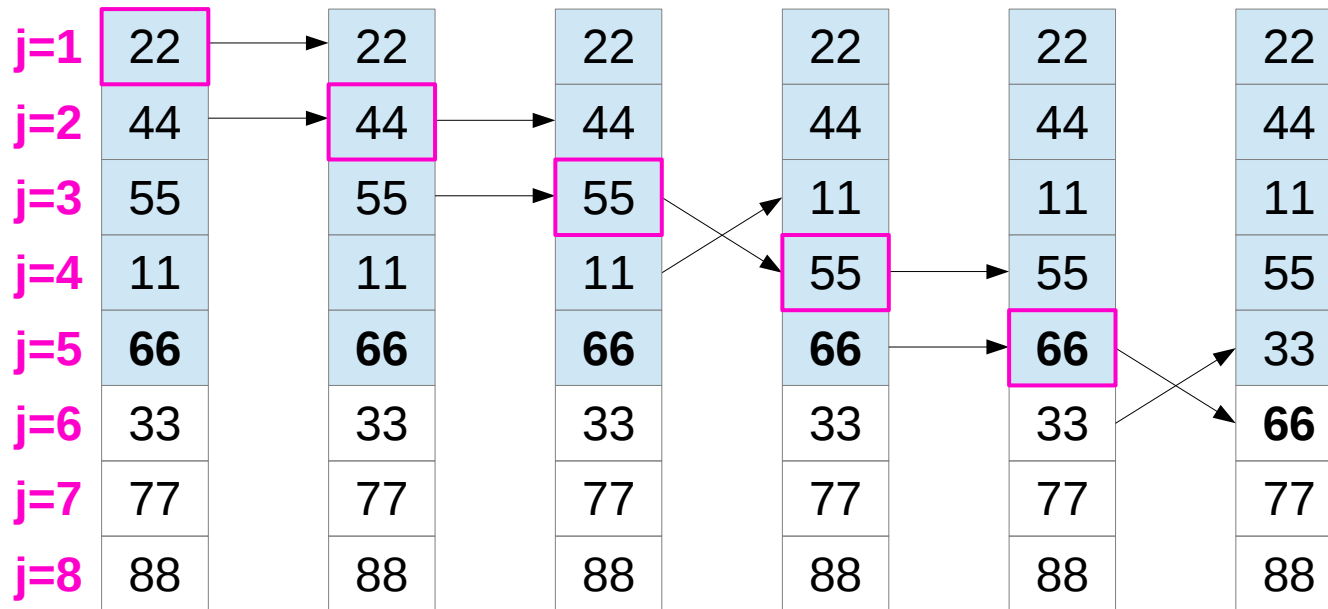
```
for i := 1 to n-1
  for j := 1 to n - i
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```

Step $i=2$



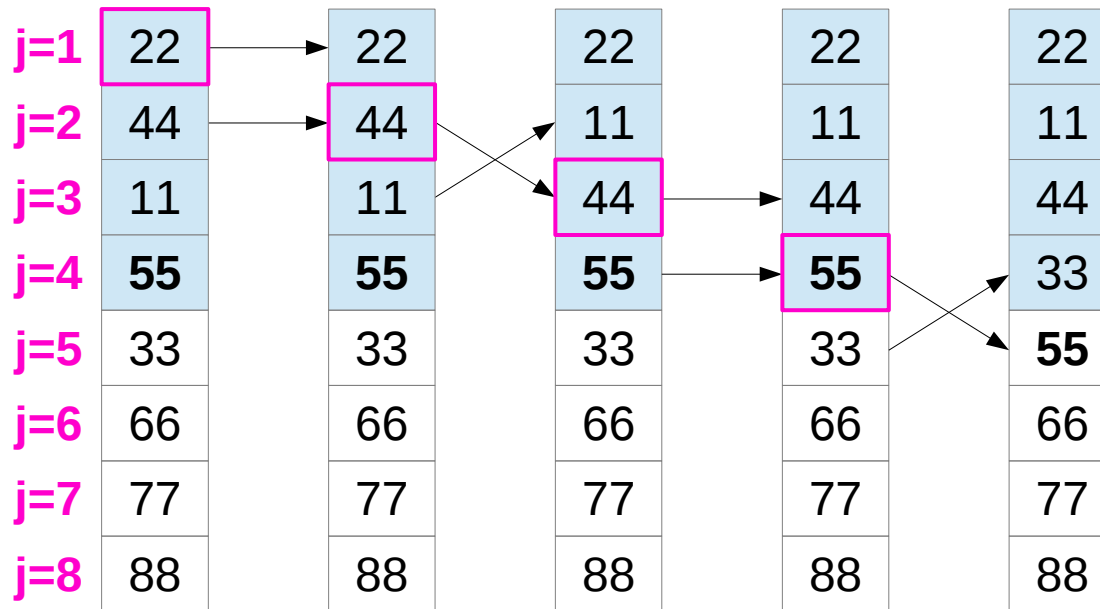
```
for  $i := 1$  to  $n-1$   
  for  $j := 1$  to  $n - i$   
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```

Step $i=3$



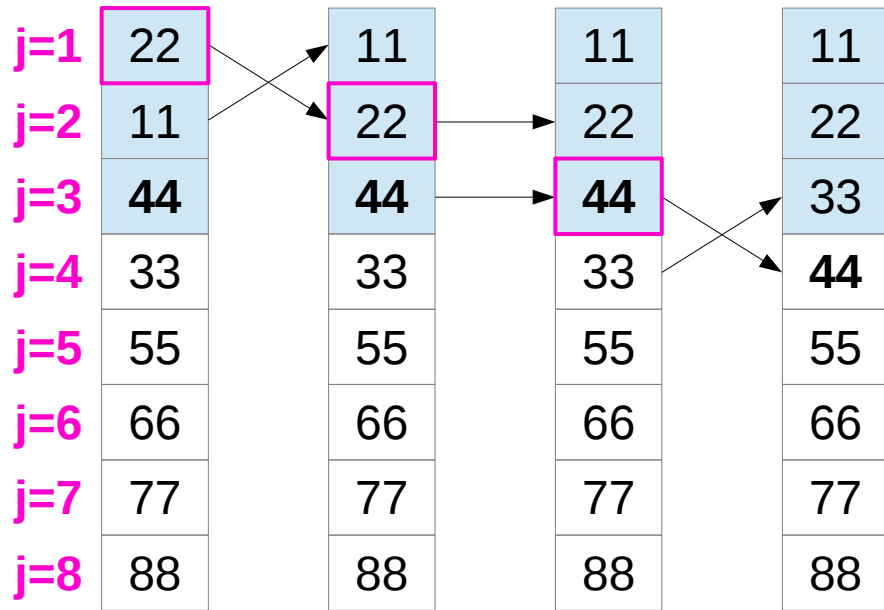
```
for  $i := 1$  to  $n-1$   
  for  $j := 1$  to  $n - i$   
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```


Step i=4



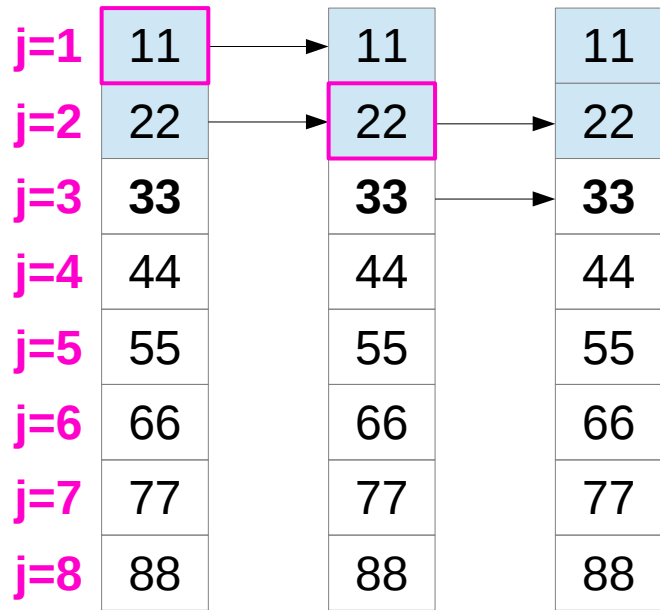
```
for i := 1 to n-1
  for j := 1 to n - i
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```

Step $i=5$



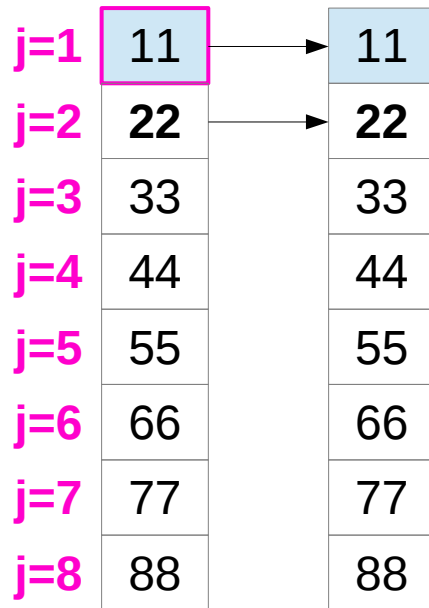
```
for i := 1 to n-1
  for j := 1 to n - i
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```

Step $i=6$



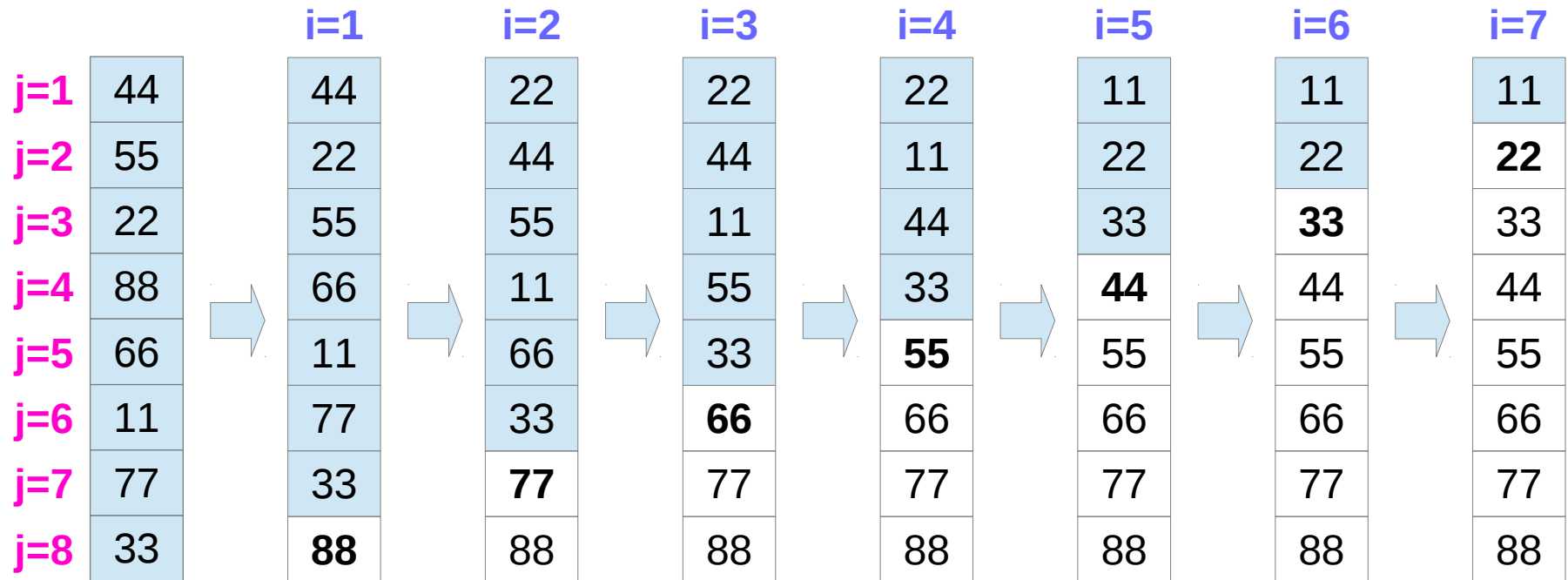
```
for  $i := 1$  to  $n-1$   
  for  $j := 1$  to  $n - i$   
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```

Step $i=7$



```
for  $i := 1$  to  $n-1$   
  for  $j := 1$  to  $n - i$   
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```

Summary



```
for i := 1 to n-1
  for j := 1 to n - i
    if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$ 
```

References

- [1] <http://en.wikipedia.org/>
- [2]